

Instructions: Show all work. Answers without work will not receive full credit. Give exact answers unless specifically asked to round.

1. Solve each of the following inequalities below and write the answer in each of the following formats: i) set notation, ii) on a number line, iii) in interval notation.

a. $3y - (5y + 2) > 4(y + 1) - 2y$

$$3y - 5y - 2 > 4y + 4 - 2y$$

$$\begin{array}{r} -2y - 2 \\ \hline -2y \end{array}$$

$$\begin{array}{r} -4y - 2 > +4 \\ +2 \quad +2 \\ \hline -4y > 6 \end{array}$$

$$\frac{-4y}{-4} > \frac{6}{-4}$$

↓
flip

$$y < -\frac{3}{2}$$

Set: $\{y \mid y < -\frac{3}{2}\}$

Line: $\leftarrow \overbrace{\hspace{2cm}}^{\frac{3}{2}} \rightarrow$

Interval: $(-\infty, -\frac{3}{2})$

b. $4(x - 1) > 3(x - 1) + x$

$$4x - 4 > 3x - 3 + x$$

$$\begin{array}{r} -4x - 4 > 3x - 3 \\ -4x \quad -3x \\ \hline -4 > -3 \end{array}$$

this is false \emptyset
no solution

Set: \emptyset

Line: $\leftarrow \overbrace{\hspace{2cm}}^{\frac{3}{2}} \rightarrow$ (empty)

Interval: none

c. $5(x - 2) < 3(x + 1) + 2x$

$$5x - 10 < 3x + 3 + 2x$$

$$\begin{array}{r} 5x - 10 < 5x + 3 \\ -5x \quad -5x \\ \hline -10 < +3 \end{array}$$

this is always true
all reals.

d. $\frac{x}{3} \geq 2 + \frac{x}{6}$

$$\frac{6x}{3} \geq 12 + \frac{6x}{6}$$

$$\begin{array}{r} 2x \geq 12 + x \\ -x \quad -x \\ \hline x \geq 12 \end{array}$$

Set: $\{x \mid x \text{ is a real } \# \}$

Line: $\leftarrow \overbrace{\hspace{2cm}}^{\frac{3}{2}} \rightarrow$ (filled in)

Interval: $(-\infty, \infty)$

Set: $\{x \mid x \geq 12\}$

Line: $\leftarrow \overbrace{\hspace{2cm}}^{12} \rightarrow$

Interval: $[12, \infty)$