

Instructions: Show all work. Answer each question as completely as possible. Use exact answers unless specifically asked to round.

1. Decompose the vector $\vec{w} = 10\hat{i} + 16\hat{j}$ into two vectors, one parallel to $\vec{v} = \hat{i} - 2\hat{j}$, and one perpendicular to it.

$$\vec{w}_1 = \frac{\vec{v} \cdot \vec{w}}{\|\vec{v}\|^2} \vec{v} = \frac{10 - 32}{5} (\hat{i} - 2\hat{j}) = -\frac{22}{5} (\hat{i} - 2\hat{j}) = -\frac{22}{5} \hat{i} + \frac{44}{5} \hat{j}$$

$$\vec{w}_2 = 10\hat{i} + 16\hat{j} - \left(-\frac{22}{5}\hat{i} + \frac{44}{5}\hat{j}\right) = \left(\frac{50}{5} + \frac{22}{5}\right)\hat{i} + \left(\frac{80}{5} - \frac{44}{5}\right)\hat{j} = \frac{72}{5}\hat{i} + \frac{36}{5}\hat{j}$$

2. Define the term "generator" in the context of a conic.

the generator is the line rotated around an axis that forms a cone.

3. How do you have to cut a cone to obtain a parabola?

with a plane at an angle parallel to a generator

4. Find the standard equation of a circle whose general form is $x^2 + y^2 + 4x + 2y + 1 = 0$. State the center of the circle and the radius.

$$(x^2 + 4x + 4) + (y^2 + 2y + 1) = -1 + 4 + 1 = 4$$

$$(x+2)^2 + (y+1)^2 = 4$$

Center $(-2, -1)$

radius = 2