### **Transformations of Graphs**

#### Learning Objectives

- Graph functions using vertical and horizontal shifts
- Graph functions using reflections about the x-axis and the y-axis
- Graph functions using compressions and stretches

Graph functions using vertical and horizontal shifts

1. Identify the graph of the function that shifts the  $y = x^3$  function one unit to the left. Write the equation of the transformation.



#### $\mathbf{\hat{f}} y$ 5 $\frac{x}{3}$ -11 $\dot{2}$ -5В. 5 $\frac{x}{1}$ -3-1\_2 -5C.

2. Which of the three functions shown on the graph below correspond to the graph of  $f(x) = x^2 - 4$ . Describe the transformation.



Graph functions using reflections about the x-axis and the y-axis

3. Identify the graph of the function below that transforms the graph of  $y = \sqrt{x}$  by reflecting it across the x-axis. Write the equation of the function.



Graph functions using compressions and stretches

4. Which of the graphs below corresponds to the function g(x) = 2|x|. Describe the transformation.



5. The graph below has applied several transformations. Identify the transformations and write the equation of the graph using transformations.



#### ANSWER KEY

1. C.,  $f(x) = (x + 1)^3$ 

2. black line (bottom), vertical shift down 4

3.  $f(x) = -\sqrt{x}$ , black line (Quadrant IV)

4. red line (top), vertical stretch by 2

5.  $f(x) = -2(x - 1)^2 + 5$ , horizontal shift right 1, reflect across the x-axis, vertical stretch by 2, vertical shift up by 5