

**Instructions:** Show all work. Give at least 4 terms for each coefficient  $a_0, a_1$  for the solution to the series.

1. Solve the differential equation using series solution methods  $xy'' - y = 0$  centered at  $x_0 = 0$ . Use the form  $y = \sum_{n=0}^{\infty} a_n x^{n+r}$  to solve the equation.

$$x \sum_{n=2}^{\infty} a_n (n+r)(n+r-1) x^{n+r-2} - \sum_{n=0}^{\infty} a_n x^{n+r} = 0$$

$$\sum_{n=2}^{\infty} a_n (n+r)(n+r-1) x^{n-1} - \sum_{n=0}^{\infty} a_n x^n = 0$$

$$\sum_{n=1}^{\infty} a_{n+1} (n+r+1)(n+r) x^n - \sum_{n=0}^{\infty} a_n x^n = 0$$

$$\sum_{n=1}^{\infty} a_{n+1} (n+r+1)(n+r) x^n - \sum_{n=1}^{\infty} a_n x^n + a_0 x^0 = 0$$

no condition on  $r$

$$\sum_{n=1}^{\infty} [a_{n+1} (n+r+1)(n+r) - a_n] x^n = 0$$

$$\Rightarrow a_0 = 0$$

$$a_{n+1} = \frac{a_n}{(n+1)(n)}$$

$$y = 0$$