

**Instructions:** This exam is in two parts: Part I is to be completed partly at home using the materials posted on Blackboard for Part I and you will answer questions about that work in class below; Part II is to be completed entirely in class. You may not use cell phones, and you may only access internet resources you are specifically directed to use. You may access your data file for Part I of the exam in Blackboard. You may access the data files posted to Blackboard for the Exam part II. Be sure you are using the data file that matches the exam version you are given.

#### Part I: At Home

This part was completed at home. You can upload the Excel file for Part I to the Part I folder in Blackboard for use during the Exam period. However, this submission will not be graded in this location, it must be submitted to the “to be graded folder” to receive credit.

#### Part II: In Class

1. Use the work done at home to answer the Part I questions.
2. Open the file from the in-class portion of the final posted on Blackboard that corresponds to the version of the exam you have. This is Exam C.
3. Answer the questions corresponding to the data file, and any additional calculation in Excel required.
4. When you have finished answering questions on the exam, and all your answers have been recorded on the paper test for grading, upload **both** the take home Excel file **and** the in-class Excel file to the same in-class Exam folder in Blackboard for grading. Only those files submitted to the correct folder will be graded. (If in doubt, put all work in one Excel file.)
5. Turn in your paper copy of the exam to your instructor.
6. Enjoy your break!



Part I:

1. Report on the results of your ANOVA test of the cereal box filling machines. State your null and alternative hypotheses, your test-statistic and P-value, and the conclusion of your test. Give a sentence to explain the meaning of the test in context understandable by a lay person. (12 points)
2. Examine your boxplots. Is the equal variance assumption approximately satisfied? Why or why not? (6 points)
3. Based on the results of your test, and the box plots, which filling machine(s) appears to be the most different from the others and is most in need of recalibration? (Or if no recalibration is needed.) Explain. (6 points)
4. Report on the findings of your  $\chi^2$ -test of independence. State the null and alternative hypotheses, your test statistic and P-value, and the conclusion. Give a sentence that summarizes the meaning of the test that a lay person can understand. (12 points)

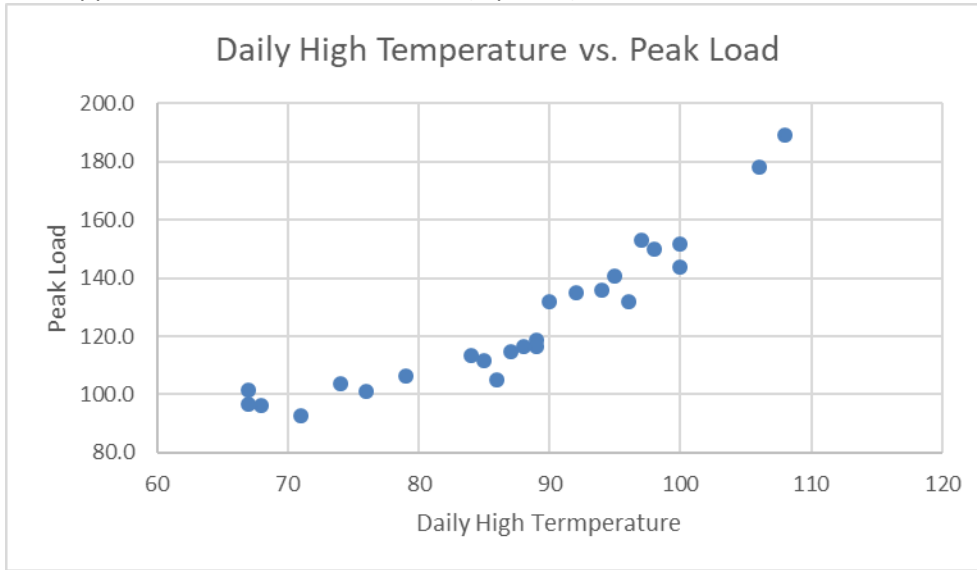


8. State your final regression equation and explain your reasoning as to why you chose this option. Report the  $R^2$  value for the equation you choose. (12 points)
9. What proportion of the variability in quantity sold can be explained by the variables you chose? (6 points)
10. Use the slope for Average Price, interpret the value of the slope in the context of the problem. (8 points)

Calculations in Excel: (1) 25 points, (2) 25 points, (3) 20 points, (4) 40 points.

Part II:

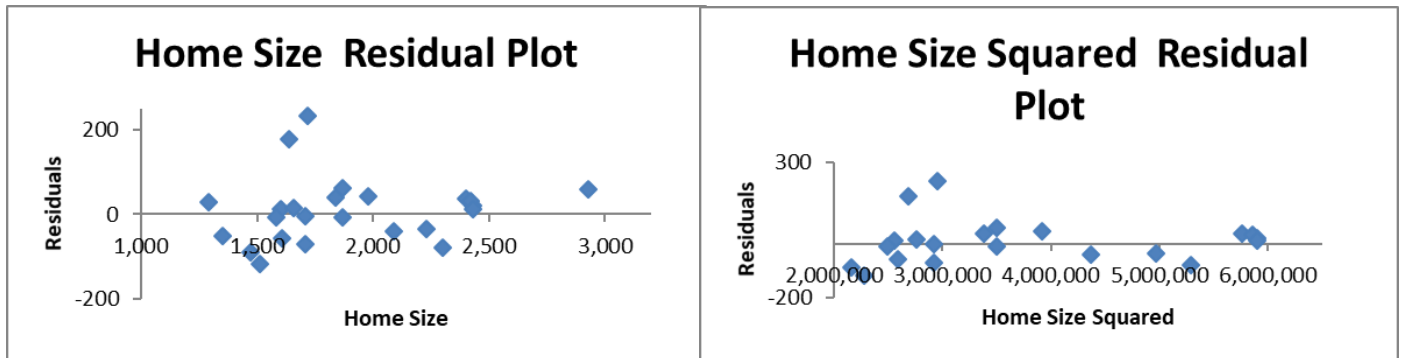
11. Included below is a scatterplot of peak load vs. daily temperature. Based on the graph, does the data appear to be linear or nonlinear? (6 points)



12. Using the trendline option on the graph, compare a linear regression line (and  $R^2$  value) with a polynomial (degree two) regression equation. Report the  $R^2$  values and equations of both and indicate which is the better model. (9 points)

13. Use the best equation to predict the peak load for an average daily temperature of  $82^\circ$  in your best equation. (6 points)

14. The regression output for the quadratic (polynomial degree-2 model) is shown on the next page along with the residual plots. Use this information to answer the questions that follow.



- a. What information do we get from residual plots? Which regression assumptions are we testing? (6 points)
- b. What is the standard error? Interpret the meaning of this value in context? (6 points)
- c. State a 95% confidence interval for the coefficient of Home Size Squared. (6 points)
- d. Conduct a hypothesis test on the coefficient of Home Size in the equation. State the hypothesis, test statistic and P-value, and interpret the results in the context of the problem. (8 points)

SUMMARY  
OUTPUT

<i>Regression Statistics</i>	
Multiple R	0.935647138
R Square	0.875435567
Adjusted R Square	0.864111527
Standard Error	91.75229367
Observations	25

ANOVA

	<i>df</i>	<i>SS</i>	<i>MS</i>	<i>F</i>	<i>Significance F</i>
Regression	2	1301627.365	650813.6827	77.30771116	1.1203E-10
Residual	22	185206.6347	8418.483394		
Total	24	1486834			

	<i>Coefficients</i>	<i>Standard Error</i>	<i>t Stat</i>	<i>P-value</i>	<i>Lower 95%</i>	<i>Upper 95%</i>	<i>Lower 90.0%</i>	<i>Upper 90.0%</i>
Intercept	-1125.35251	407.813232	-2.759480129	0.011438868	-1971.105388	-279.5996314	-1825.626707	-425.0783128
Home Size	2.346800787	0.412042263	5.695534167	9.96046E-06	1.492277435	3.201324139	1.639264733	3.054336841
Home Size Squared	-0.000449192	0.000100737	-4.459039505	0.000196587	-0.000658108	-0.000240275	-0.000622172	-0.000276211



**Standard errors:**  $\sigma_{\bar{x}} = \frac{\sigma}{\sqrt{n}}$   $\sigma_{\hat{p}} = \sqrt{\frac{p(1-p)}{n}}$   $S_{pooled} = \sqrt{\frac{(n_1-1)s_1^2 + (n_2-1)s_2^2}{n_1+n_2-2}}$

$$S_{x_1-x_2} = S_{pooled} \sqrt{\frac{1}{n_1} + \frac{1}{n_2}}$$

**Sample sizes:**  $n > \hat{p}(1-\hat{p}) \left(\frac{z_{\alpha/2}}{E}\right)^2$   $n > \left(\frac{z_{\alpha/2}\sigma}{E}\right)^2$   $m = n = \frac{4z_{\alpha/2}^2(\sigma_1^2 + \sigma_2^2)}{w^2}$

**Confidence intervals:**

One sample:  $\bar{x} \pm t_{\alpha/2, n-1} \frac{s}{\sqrt{n}}$   $\hat{p} \pm z_{\alpha/2} \sqrt{\frac{\hat{p}(1-\hat{p})}{n}}$

Two samples (independent):  $(\bar{x}_1 - \bar{x}_2) \pm t_{\alpha/2, n-1} \sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}$   $(\hat{p}_1 - \hat{p}_2) \pm z_{\alpha/2} \sqrt{\frac{\hat{p}_1(1-\hat{p}_1)}{n_1} + \frac{\hat{p}_2(1-\hat{p}_2)}{n_2}}$

**Test statistics:**

One sample:  $z$  or  $t = \frac{\bar{x} - \mu_0}{s/\sqrt{n}}$   $Z = \frac{\hat{p} - p_0}{\sqrt{p_0(1-p_0)/n}}$

Two samples: dependent:  $z$  or  $t = \frac{\bar{d}_0 - \delta}{\frac{s_d}{\sqrt{n}}}$

Independent:  $z$  or  $t = \frac{(\bar{x}_1 - \bar{x}_2) - (\mu_1 - \mu_2)}{\sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}}$   $Z = \frac{(\hat{p}_1 - \hat{p}_2) - (p_1 - p_2)}{\sqrt{\frac{p_1(1-p_1)}{n_1} + \frac{p_2(1-p_2)}{n_2}}}$

Degrees of freedom (two samples, unpooled)  $\nu = \frac{\left(\frac{s_1^2}{m} + \frac{s_2^2}{n}\right)^2}{\frac{\left(\frac{s_1^2}{m}\right)^2}{m-1} + \frac{\left(\frac{s_2^2}{n}\right)^2}{n-1}}$

$\chi^2$  Tests:  $\chi^2 = \sum_{all\ cells} \frac{(obs - exp)^2}{exp}$

ANOVA:  $MSE = \frac{(\sum_{j=1}^J n_j (\bar{Y}_j - \bar{Y})^2)}{J-1}$   $MSS = \sum_{j=1}^J \frac{(n_j - 1) s_j^2}{n - J}$   $F = \frac{MSE}{MSS}$

Upload your completed Excel files to the Exam #2 submission box in Blackboard, and submit your completed paper exam to your instructor. You may not modify anything once the exam is submitted.