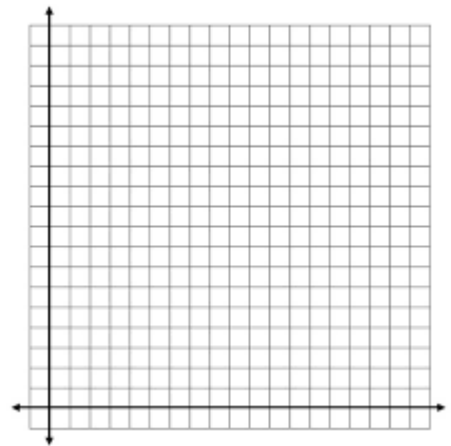


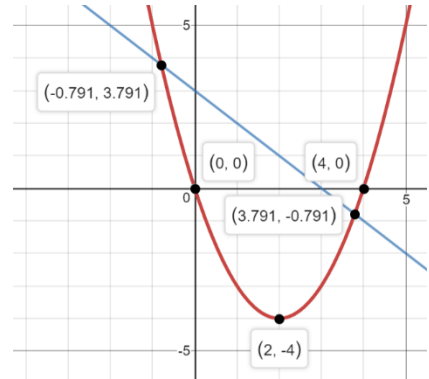
MTH 161, Practice Exam #2, Spring 2019

1. Is $x = -2$ a solution to the inequality $\frac{2-3x}{x-2} > 0$? Explain.
2. The inequality $x^2 + 1 < 0$ has no real solution. Explain why.
3. Give an example of a rational function with a vertical asymptote at $x = 1$ and a horizontal asymptote at $y = 2$.
4. Use the intermediate value theorem to show that the function $f(x) = -2x^2 + 5x + 11$ has a real zero on the interval $[2,4]$.
5. Find the partial fraction decomposition of $\frac{2x-1}{x^2-4x-12}$.
6. Given the following polynomial function, $f(x) = \frac{1}{2}(x-1)^3(x+3)^2(x^2+4)$.
 - a. Identify the real zeros and multiplicity.
 - b. How does the function behave at each zero (touch, cross, etc.)
 - c. The graph behaves like the function $y = \underline{\hspace{2cm}}$ for large values of $|x|$.
7. Use long division to find $\frac{x^5-4x^3+x^2+1}{x^2-2x-3}$. Write your final answer as $q(x) + \frac{r(x)}{d(x)}$.
8. A toy store has 30 meters of fencing to fence off a rectangular area for an electric train display in one corner of the store. Two sides are against the wall and will need no fence.
 - a. Write an equation that represents the total length of fence in terms of W and L . (Let $L = x$.)
 - b. Write an equation that represents the area of $A(x)$.
 - c. Find the maximum area and give the dimensions.
 - d. Sketch the graph of $A(x)$, label and use an appropriate domain and range.
9. Solve the inequalities, showing sign charts for each.
 - a. $2x(x-1)^2(3-x) < 0$
 - b. $\frac{3-x}{x+1} \geq 2$



10. Consider the graph $f(x)$ and $g(x)$ to the right.

- $f(x) = g(x)$
- $f(x) < g(x)$
- $f(x) = 0$



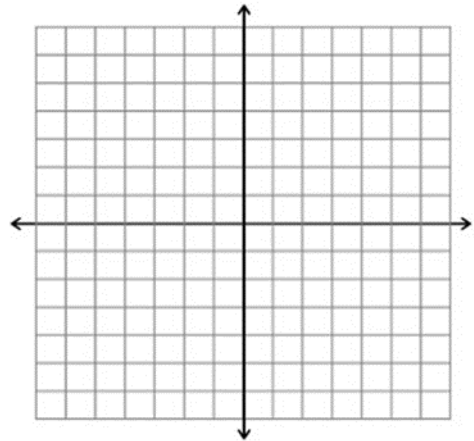
11. Consider the polynomial function

$$f(x) = x^5 + 3x^4 - 9x^3 - 21x^2 - 10x - 24$$

- Based on degree, how many real zeros and complex zeros does f have?
- Using the Rational Zeros Theorem, list the possible rational zeros of f .
- Use synthetic division to show that $x = -2$ is a zero of f .
- Finish factoring the polynomial. Write as a product of linear factor with complex numbers where appropriate.
- List all real and imaginary zeros of the function.

12. Consider the rational function $f(x) = \frac{9-3x}{2+x}$. Find the following properties of the function. If it does not apply, write DNE.

- Holes
- Vertical asymptote(s)
- Horizontal asymptote
- Domain
- X-intercept(s)
- Y-intercept
- Sketch the graph, labeling each element from the list above.



13. What value should you write in the circle to check whether $(x + 4)$ is a factor of $f(x) = x^3 - 2x^2 + 3x + 4$?

| 1 - 2 3 4

14. What feature of the graph of $y = \frac{5}{x-3}$. What can you find by solving $x - 3 = 0$?

15. Is $y = \frac{2}{3}$ a horizontal asymptote of $y = \frac{2x}{3x^2-9}$.

16. If a zero of a polynomial f is of odd multiplicity, then the graph of f _____ the x-axis at that zero.
17. Suppose that $-2 + i$ is a zero of a polynomial function. This implies that _____ is also a zero.
18. If $x = -3$ is a zero of a polynomial function f , then _____ is a factor of the polynomial $f(x)$.